



**TFAWS**  
LaRC 2019

## Numerical Simulation of Transient Behavior of Vapor-Liquid Distribution in a Loop Heat Pipe

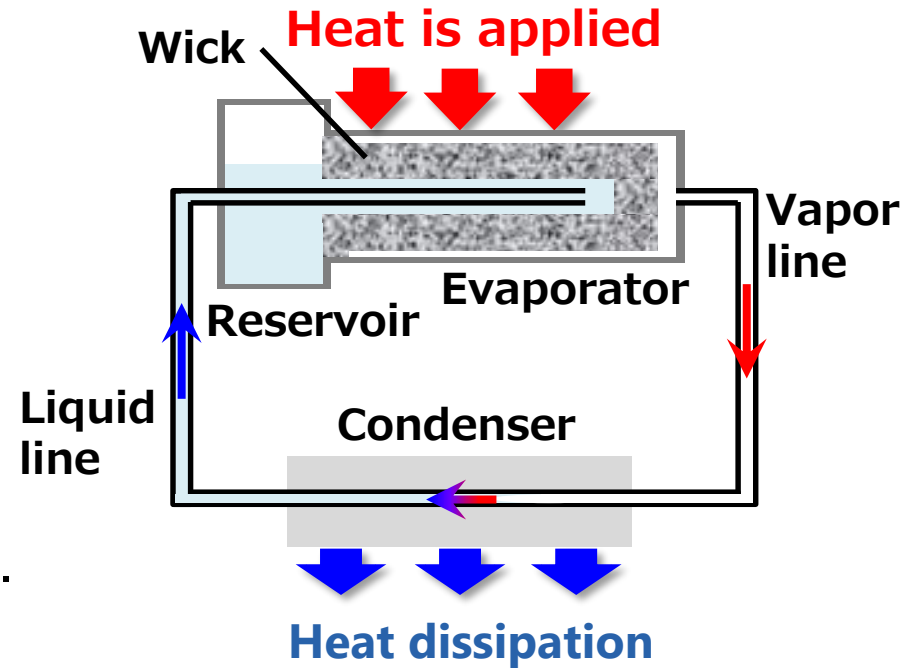
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TFAWS 2019  
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NASA Langley Research Center  
Hampton, VA

- Advantages

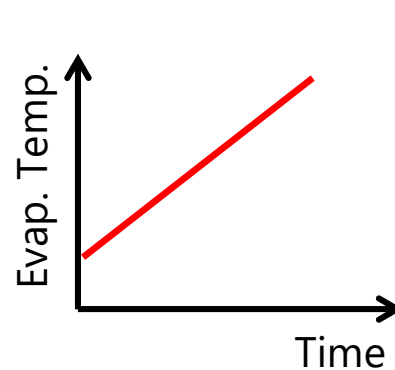
- Heat transportation by the latent heat
  - Transporting a lot of heat
  - Long distance transport
- Capillary force of the wick circulates the working fluid.
  - No electric power is required.
- Shutdown



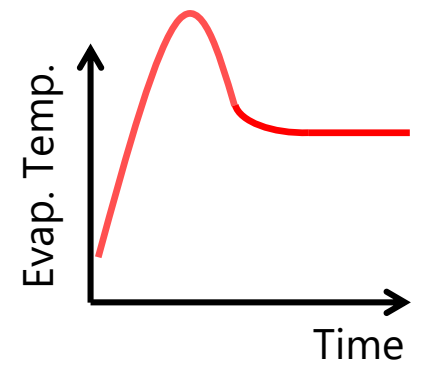
- Problem: **Unstable Startup**

- Failure of startup
- High temperature peak
- Long time to convergence

**Startup characteristics have to be understood.**

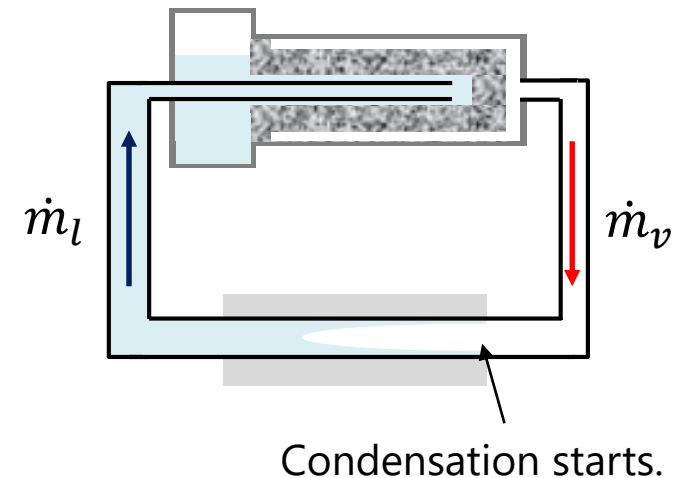


**Failure of startup**



**High temp. peak**

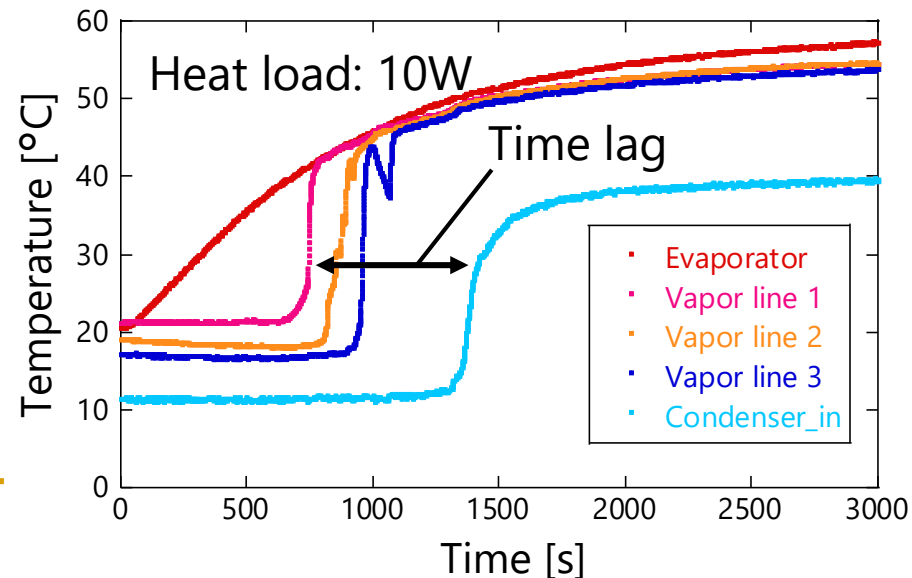
- Simplifying flow in transport lines
  - The mass flow rate in the vapor line and in the liquid line are respectively constant.
  - Condensation always starts at the condenser inlet.



As soon as evaporation occurs, the cond. inlet temp. would rise.

- Temperature distribution during startup cannot be accurately reproduced.

**It is necessary to accurately reproduce the energy propagation in the transport lines.**



- Volume of fluid (VOF) method

- Void fraction transport equation

$$\rho_v \frac{\partial \alpha_v}{\partial t} + \rho_v \frac{\partial (u \alpha_v)}{\partial x} = \underline{S_{\alpha_v}}$$

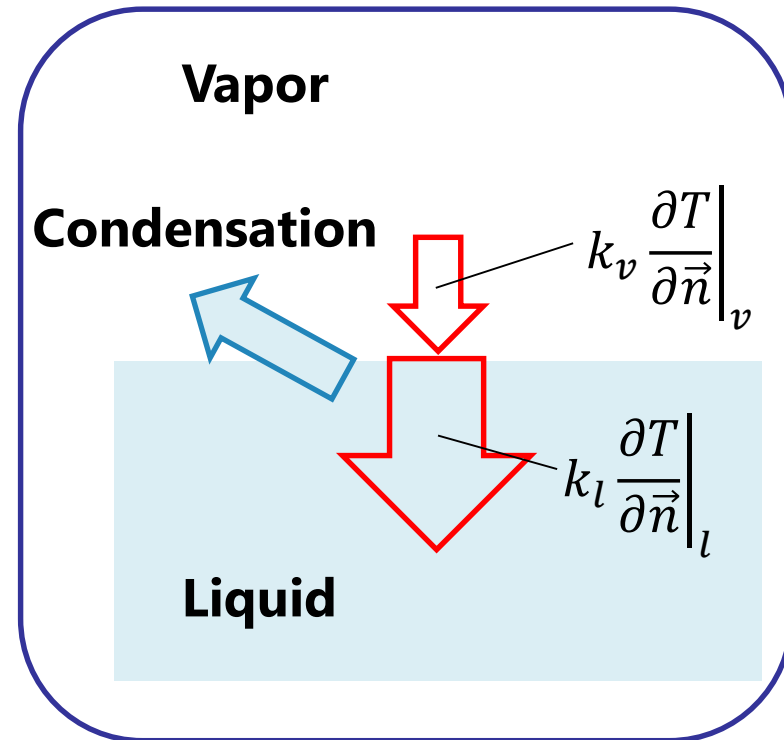
Mass source term

- Mass source term:  
Amount of phase-change

$$S_{\alpha_v} = \left( k_l \frac{\partial T}{\partial \vec{n}} \Big|_l - k_v \frac{\partial T}{\partial \vec{n}} \Big|_v \right) \frac{A_{int}}{h_{lv} \cdot V}$$

- Various condensation flow can be reproduced.
- Calculation cost is high.

**One-dimensional modeling is required to investigate the startup characteristics.**



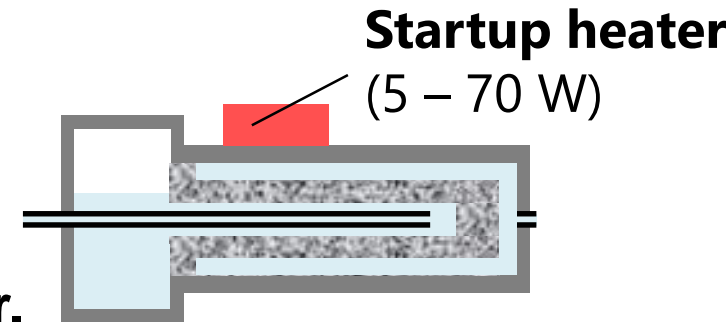
$A_{int}$  : interface area  
 $h_{lv}$  : latent heat  
 $k$  : conductivity  
 $T$  : temperature  
 $u$  : velocity  
 $\alpha_v$  : void fraction  
 $V$  : volume

# Vapor-liquid distribution in transport lines

- General solution of startup failure

- The startup heater is attached to the evaporator.

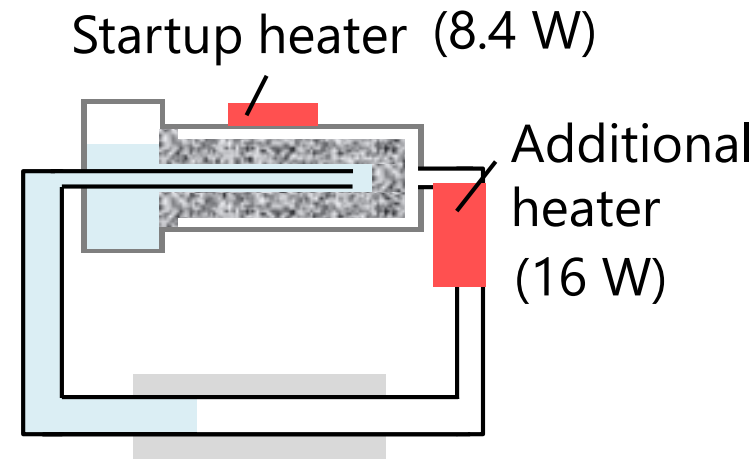
→ **Nucleation boiling is easy to occur.**



- Failure of startup heater

- The additional startup heater is required on the vapor line to start the LHP's operation

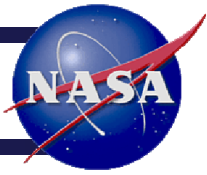
→ **Vapor-liquid distribution in the transport lines would affect the startup characteristics.**



The model that can investigate the influence of the vapor-liquid distribution in the transport lines is necessary to understand startup characteristics.

## **Developing the one-dimensional model of an LHP to investigate the startup characteristics.**

- Reproducing the accurate energy propagation in the transport lines by using the Volume of fluid method.
- Modeling the condensation in one dimension.



# Numerical model

- Evaporator

- The evaporation occurs as soon as heat is applied.

- Reservoir

- Fluid is always saturated.
- Amount of liquid in reservoir is the remainder of liquid in the transport lines.

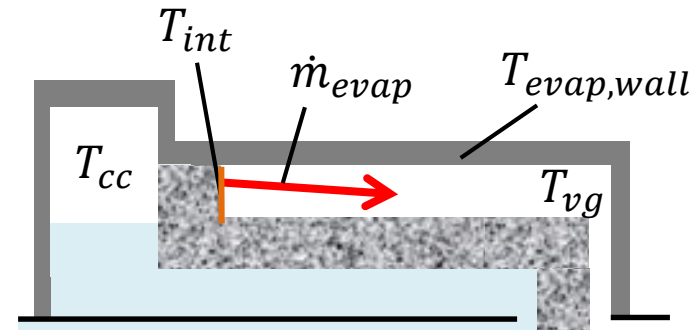
- Amount of evaporation

- Tanasawa's simplified model

$$\dot{m}_{evap} = \frac{2\gamma}{2 - \gamma} \sqrt{\frac{M}{2\pi R}} \left[ \frac{\rho_v h_{lv} (T_{vg} - T_{int})}{T_{sat}^{3/2}} \right]$$

- $\gamma = 0.01$  is used for the calculation.
- $T_{int}$ : vapor-liquid interface temperature

$$T_{int} = T_{sat}(P_{vg})$$

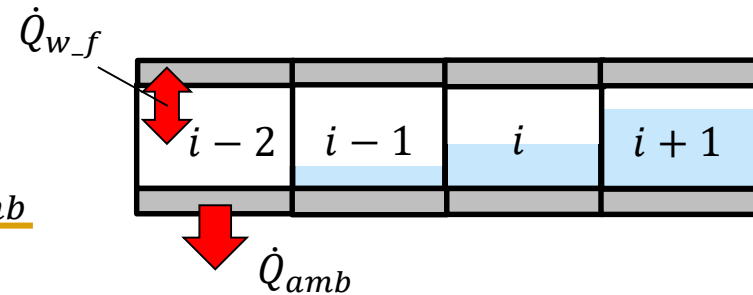


$\dot{m}_{evap}$	: amount of evaporation [kg/s]
$\gamma$	: accommodation coefficient
$T_{evap,wall}$	: evap. wall temp. [K]
$T_{int}$	: interface temp. [K]
$h_{lv}$	: latent heat [J/kg]
$h_{evap}$	: heat transfer coef. [W/(m <sup>2</sup> *K)]
$A_{wick}$	: contact area [m <sup>2</sup> ]
$M$	: molecular weight [kg/mol]
$R$	: gas constant [J/K/mol]



- Heat conduction equation

$$\rho_{wall} c_{p_{wall}} \frac{\partial T_{wall}}{\partial t} = k_{wall} \frac{\partial^2 T_{wall}}{\partial x^2} - \dot{Q}_{w\_f} + \dot{Q}_{amb}$$



- Momentum conservation equation

$$\frac{\partial(\rho_f u)}{\partial t} + \frac{\partial(\rho_f u u)}{\partial x} = -\frac{\partial p}{\partial x} + \frac{\partial}{\partial x} \left( \mu_f \frac{\partial u}{\partial x} \right) - \frac{\xi}{d_{in}} \frac{1}{2} \rho_f u_i^2$$

Pressure  
drop

- Mass conservation

$$\frac{\partial(\rho_f u)}{\partial x} = 0$$

- Energy conservation equation

$$\rho_f c_{p_f} \frac{\partial T_f}{\partial t} + \rho_f c_{p_f} \frac{\partial T_f}{\partial x} = \frac{\partial}{\partial x} \left( k_f \frac{\partial T_f}{\partial x} \right) + \dot{Q}_{w\_f} + \underline{S_v \cdot h_{lv}}$$

Heat generation by phase change

## Nomenclature

$c_p$	: specific heat [kg/m <sup>2</sup> /s]
$d_{in}$	: diameter [m]
$h_{lv}$	: latent heat [J/kg]
$k$	: thermal conductivity [W/(m·K)]
$p$	: pressure [Pa]
$\dot{Q}$	: heat flow [W/m <sup>3</sup> ]
$T$	: temperature [K]
$u$	: velocity [m/s]
$\mu$	: viscosity [Pa·s]
$\xi$	: Darcy friction coefficient [-]
$\rho$	: density [kg/m <sup>3</sup> ]

- Void fraction transport equation

$$\rho_v \frac{\partial \alpha_v}{\partial t} + \rho_v \frac{\partial (u \alpha_v)}{\partial x} = \underline{S_{\alpha_v}}$$

$A_{int}$  : interface area  
 $h_{lv}$  : latent heat  
 $k$  : conductivity  
 $T$  : temperature  
 $u$  : velocity  
 $\alpha_v$  : void fraction  
 $V$  : volume

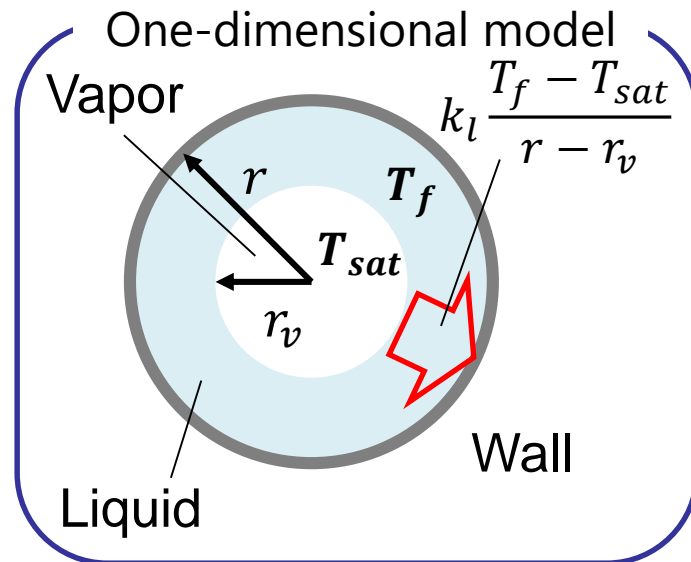
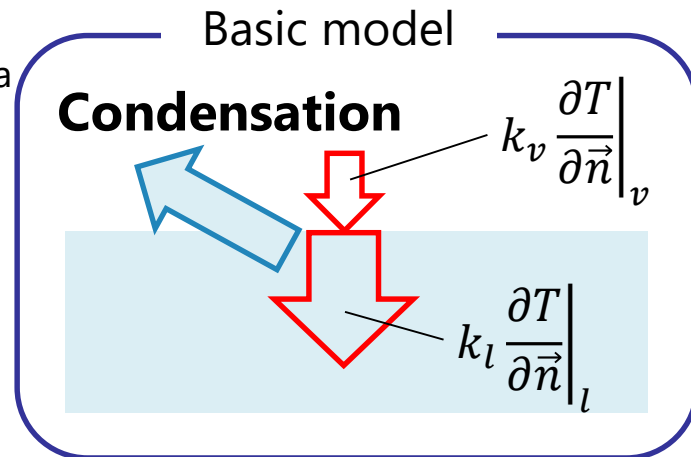
- Amount of condensation

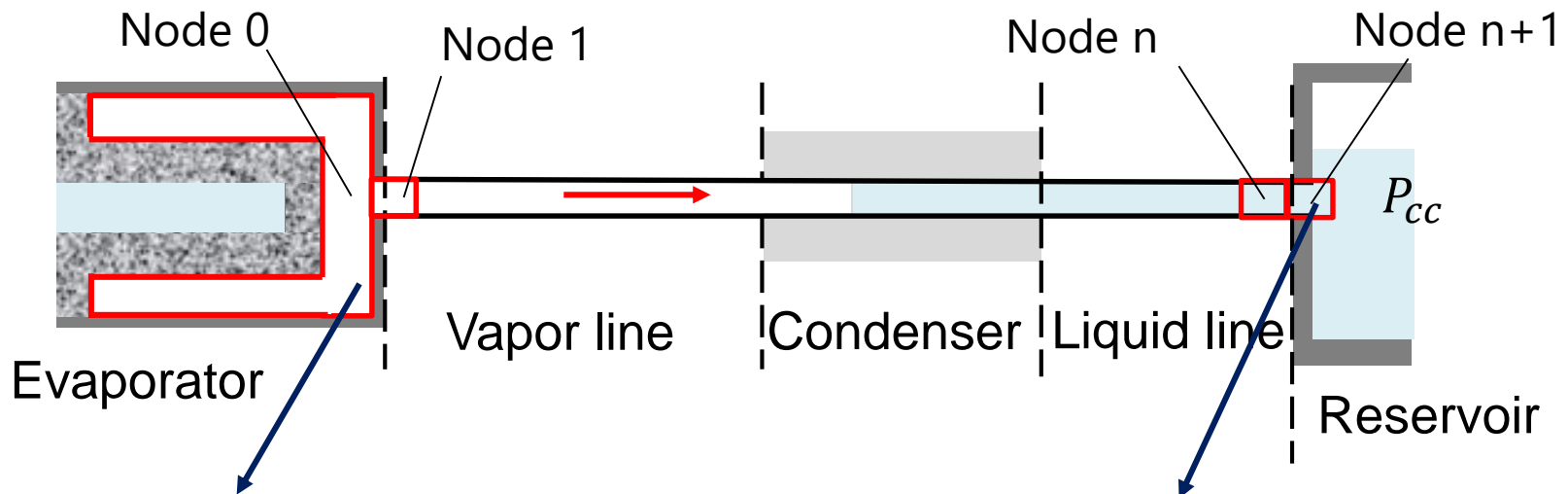
$$S_{\alpha_v} = \left( k_l \frac{\partial T}{\partial \vec{n}} \Big|_l - k_v \frac{\partial T}{\partial \vec{n}} \Big|_v \right) \frac{A_{int}}{h_{lv} \cdot V}$$

- One-dimensional model

- Vapor: Saturation temperature based on pressure ( $T_{sat}$ )
- Liquid: Temperature from the energy equation ( $T_f$ )

$$S_{\alpha_v} = k_l \frac{T_f - T_{sat}}{r - r_v} \cdot \frac{A_{int}}{h_{lv} \cdot V}$$





$$u_0 = u_{vg}$$

- $u_{vg}$  is calculated from  $\dot{m}_{evap}$ .

$$P_0 = P_1$$

$$T_{wall,0} = T_{evap,wall}$$

$$T_{fluid,0} = T_{vg}$$

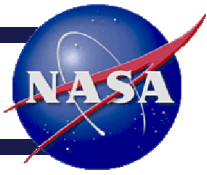
$$u_{n+1} = u_n$$

$$P_{n+1} = P_{cc}$$

- $P_{cc}$  is calculated as the saturation pressure.

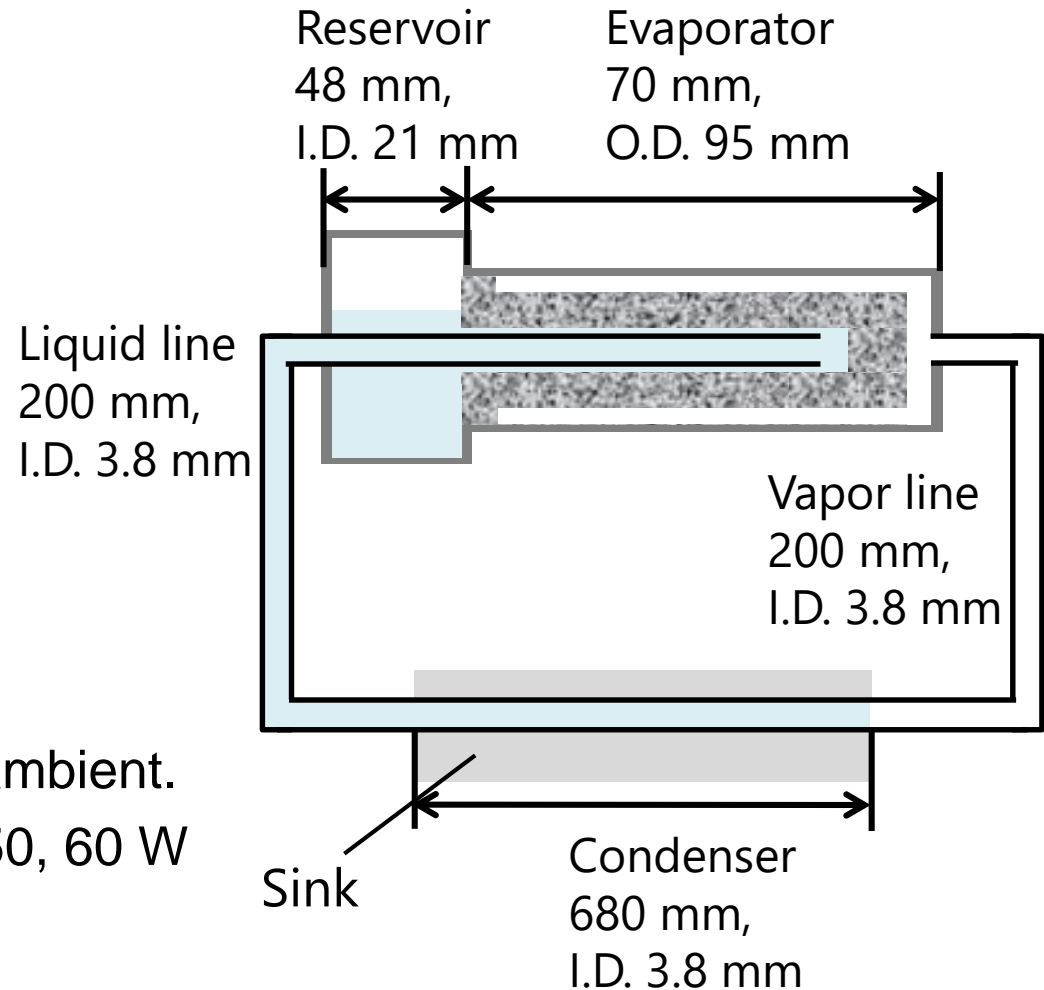
$$T_{wall,n+1} = T_{cc}$$

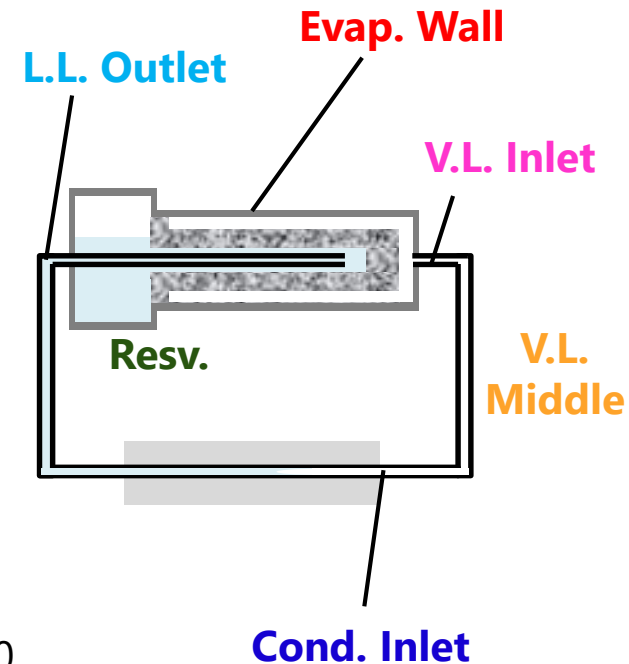
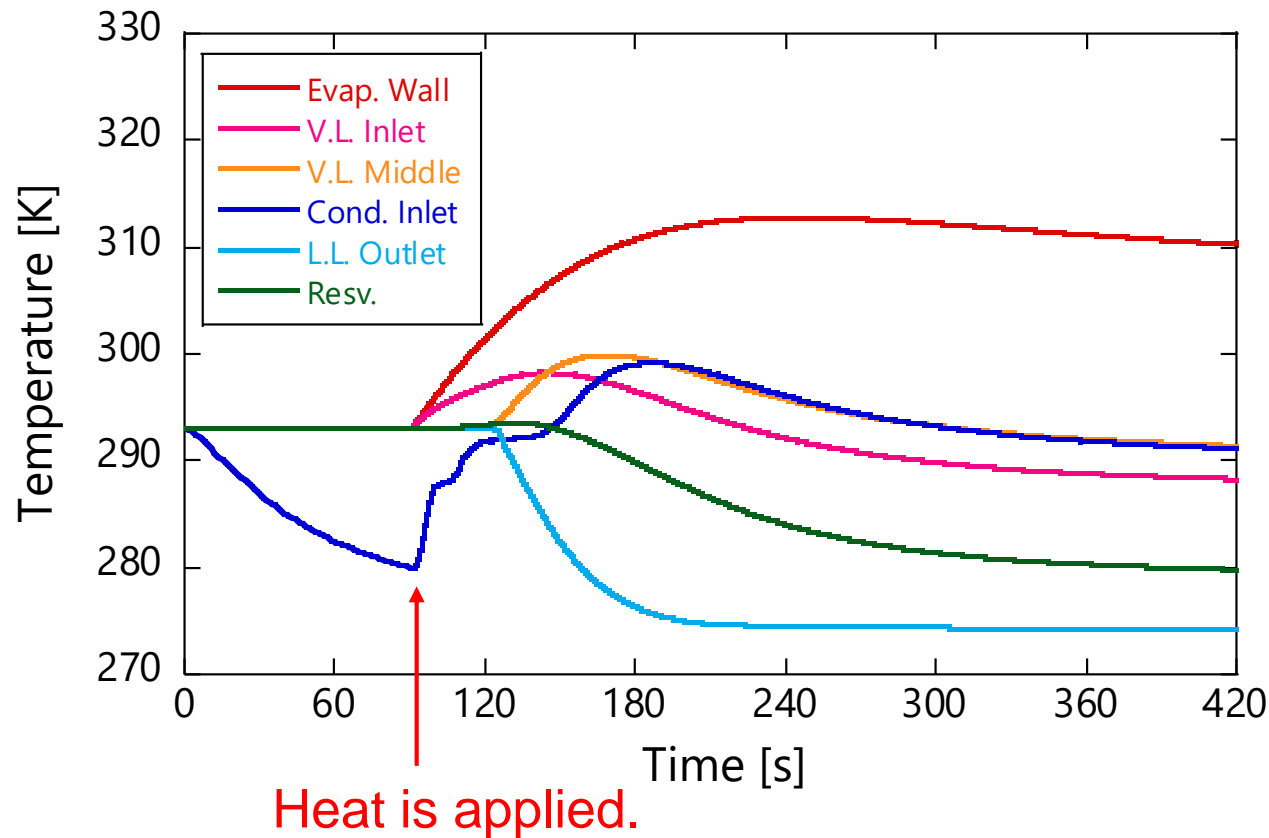
$$T_{fluid,n+1} = T_{cc}$$



# Calculation results

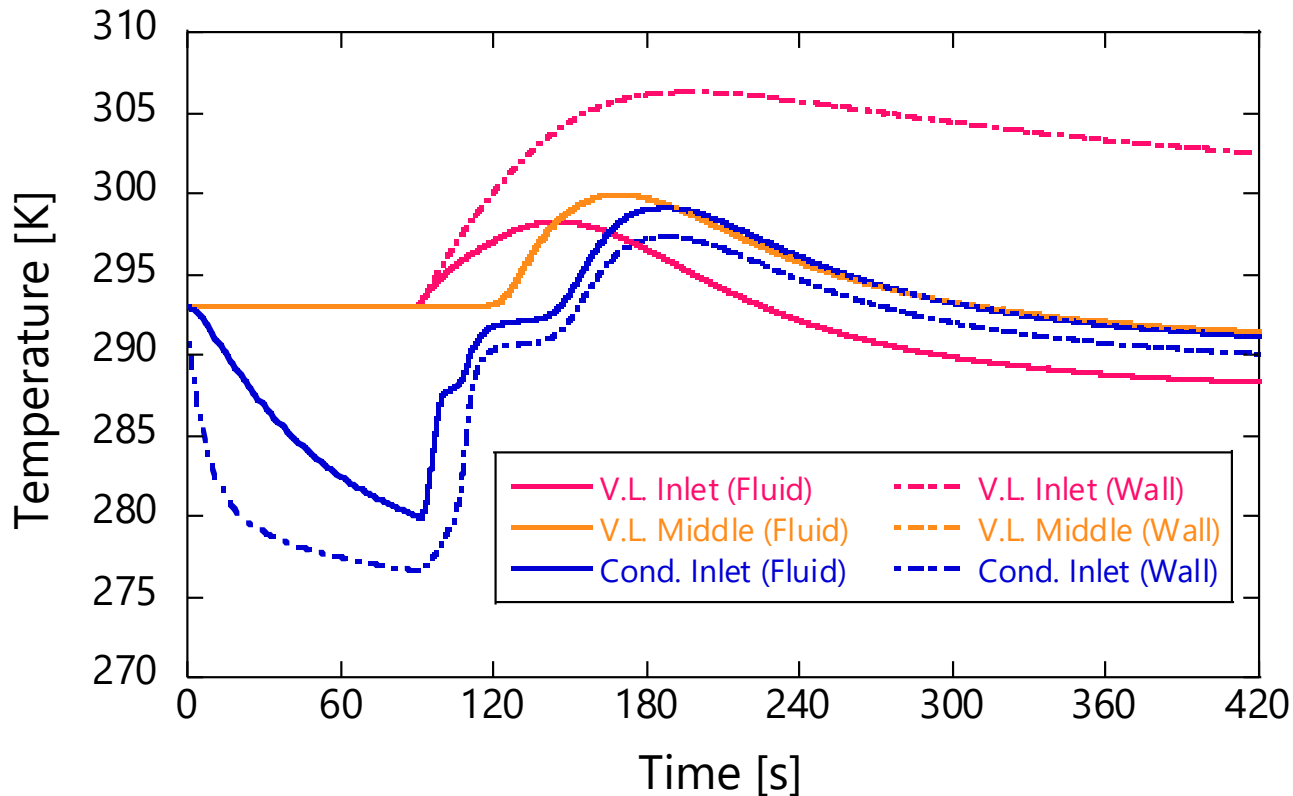
- **Wick**
  - PTFE wick
  - Pore diameter: 1  $\mu\text{m}$
  - Porosity: 0.5
- **Working fluid**
  - Acetone
  - Filling ratio: 50 vol.%
- **Boundary condition**
  - Sink temperature: 0  $^{\circ}\text{C}$
  - LHP is insulated from ambient.
  - Heat load: 10, 20, 40, 50, 60 W
- **Initial condition**
  - Initial temperature: 20  $^{\circ}\text{C}$





- There is a difference in the time when the temperature rises in the V.L.
- V.L. Inlet temperature is lower than Cond. Inlet temperature.

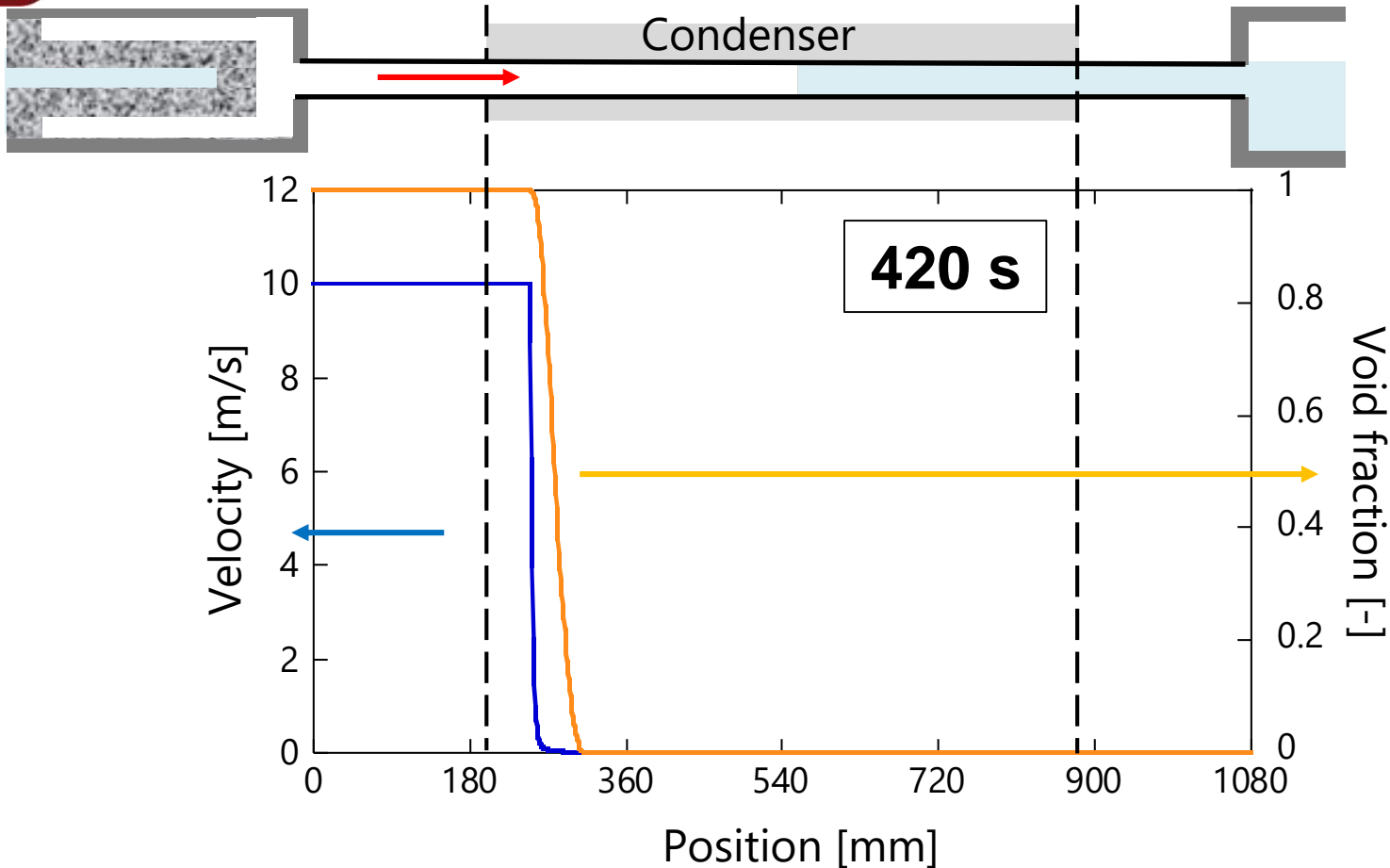
# Time lag between fluid and wall



- There is a difference between the time when the wall temperature rises and the time when the fluid temperature rises at Cond. Inlet.
- Fluid temperature is the same as the wall temperature at V.L. Middle.

**The cause of time lag is not heat capacity of the pipe wall.**

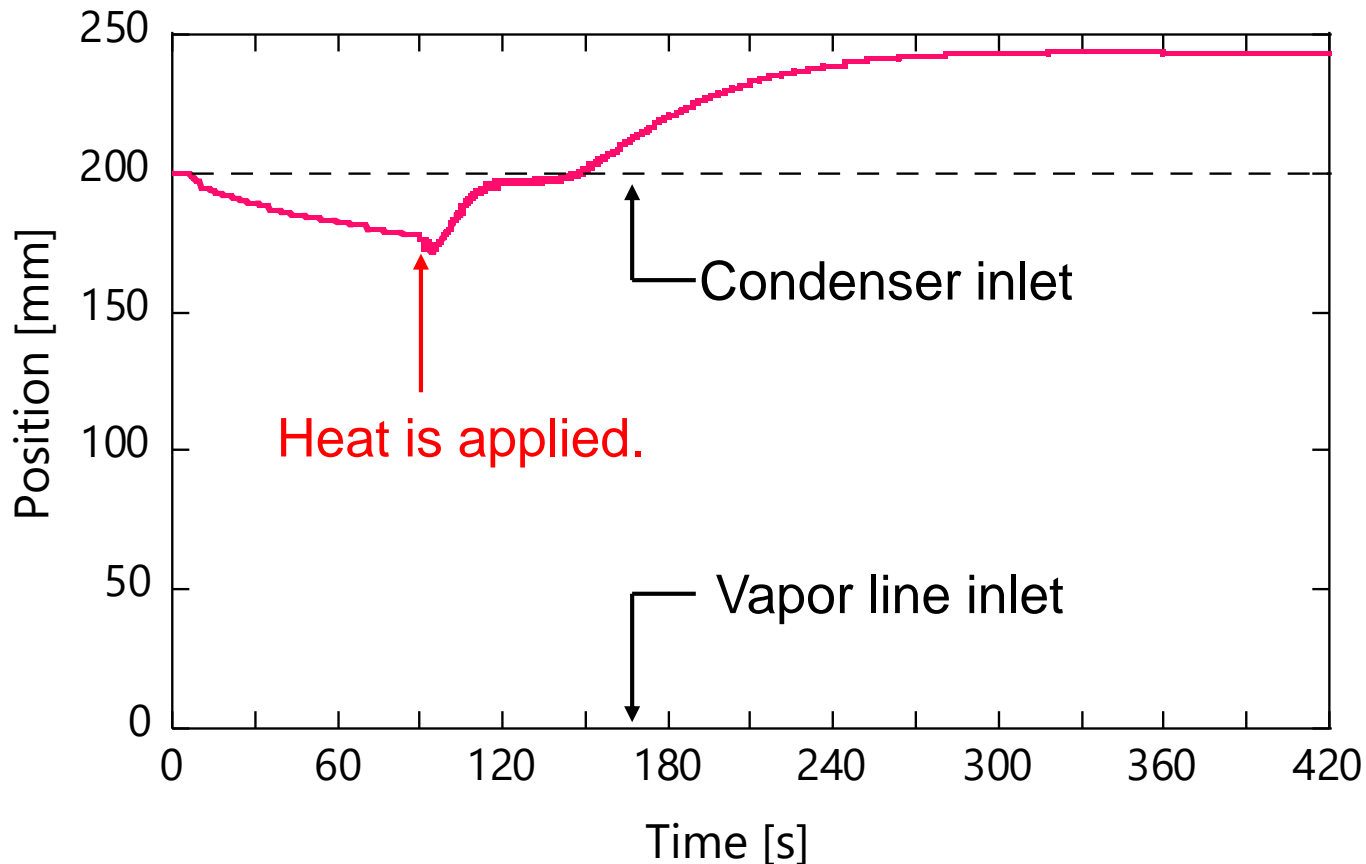
# Velocity and void fraction distribution



- Vapor penetrates the condenser.
- Vapor completely condenses in the condenser.
- Velocity of the vapor is almost constant.



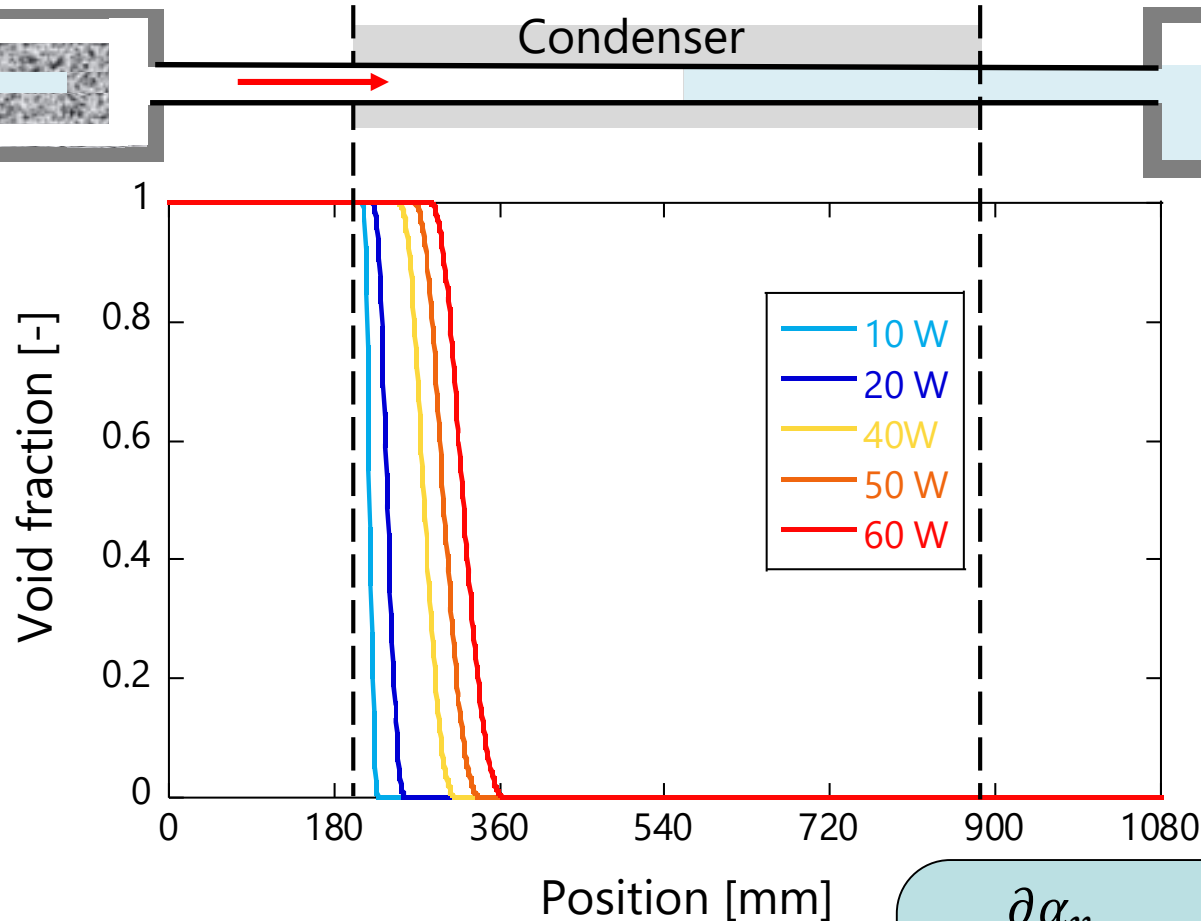
# The position where condensation starts



- Vapor is condensed in the condenser.
- Condensation does not start at the condenser inlet.

**This model can investigate the position where condensation starts.**

# Void fraction distribution

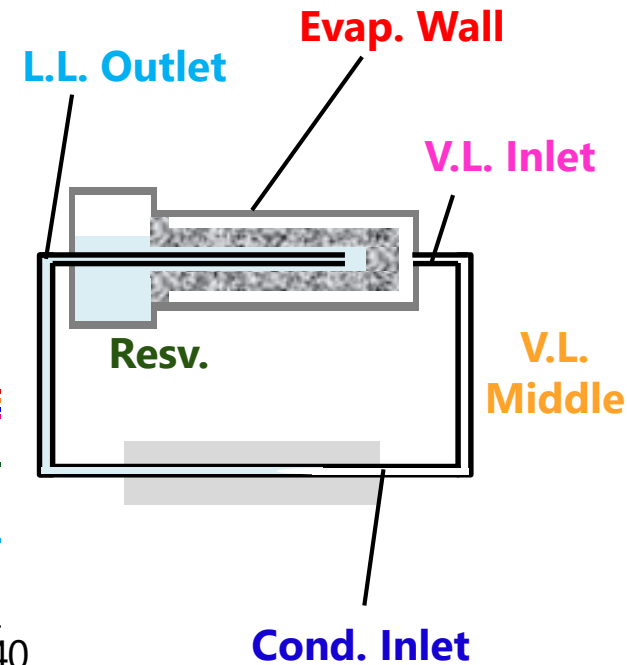
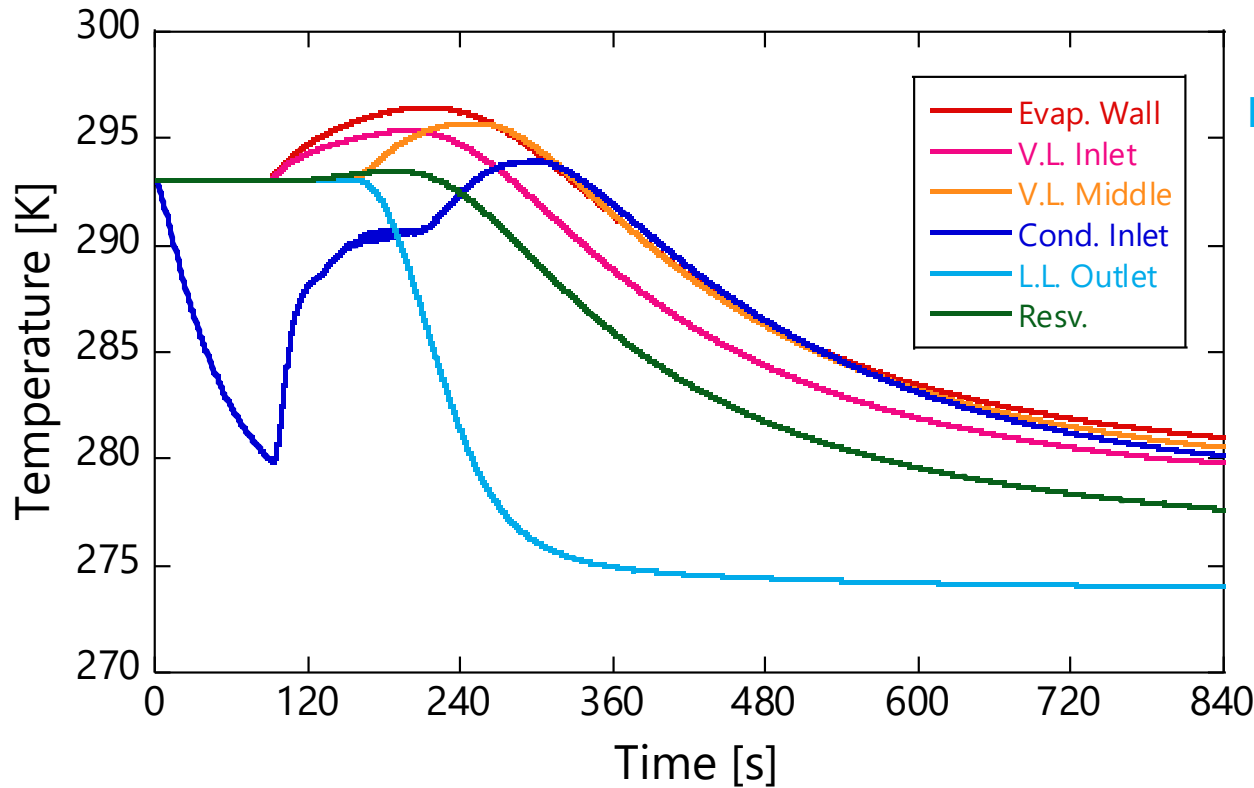


- The tilt of each heat load is almost same.
- Two-phase length is very short.

**Mass source term should be revised.**

$$\rho_v \frac{\partial \alpha_v}{\partial t} + \rho_v \frac{\partial (u \alpha_v)}{\partial x} = \underline{S_{\alpha_v}}$$

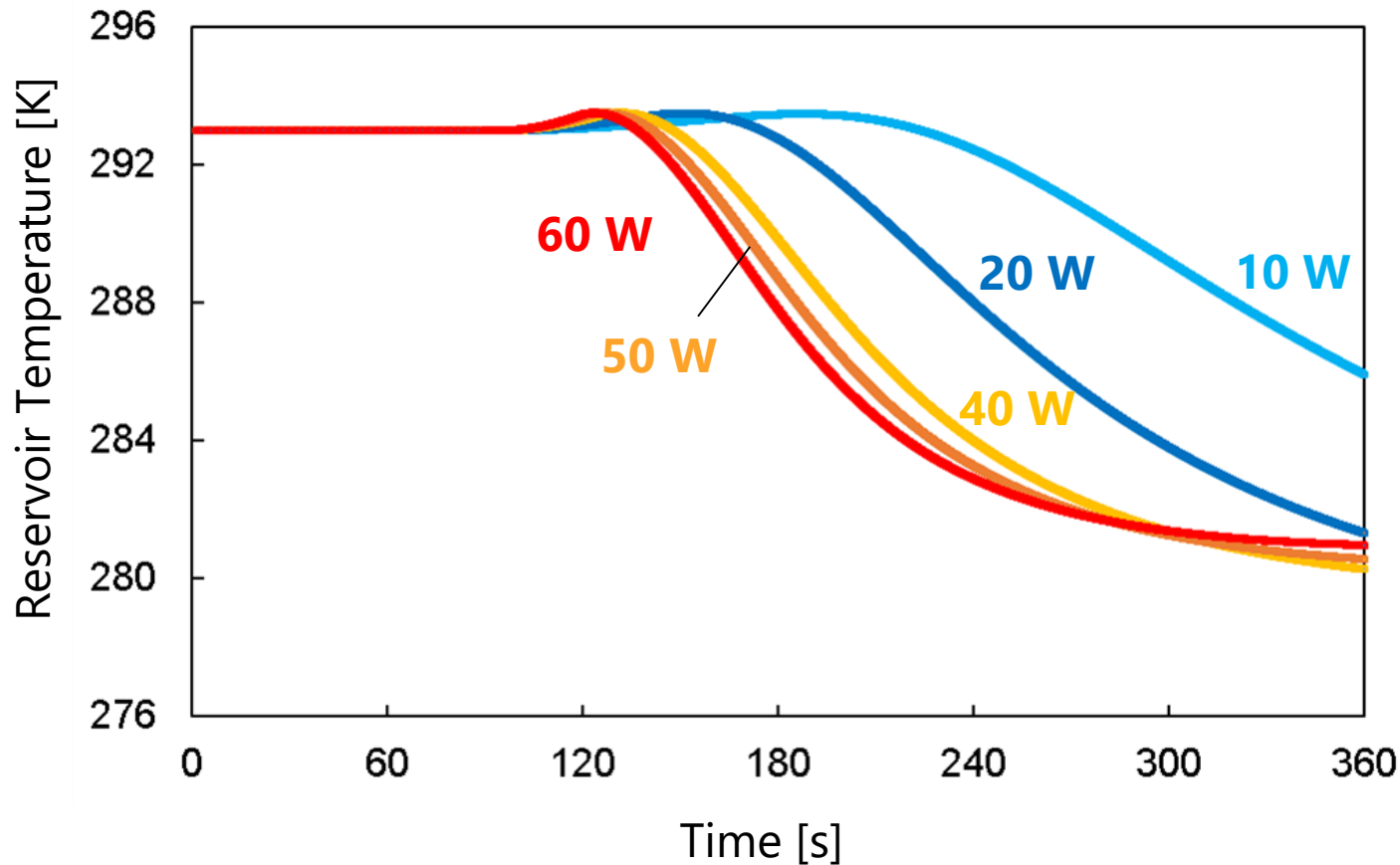
$$S_{\alpha_v} = k_l \frac{T_f - T_{sat}}{r - r_v} \cdot \frac{A_{int}}{h_{lv} \cdot V}$$



- Cond. inlet temperature becomes higher than Evap. wall temperature.  
Cause: heat generation by phase change at Cond. inlet

$$\rho_f c_{p_f} \frac{\partial T_f}{\partial t} + \rho_f c_{p_f} \frac{\partial T_f}{\partial x} = \frac{\partial}{\partial x} \left( k_f \frac{\partial T_f}{\partial x} \right) + \dot{Q}_{w-f} + \underline{S_v \cdot h_{lv}}$$

**Condensation model needs modification.**



- Reservoir temperature decreases due to the returning liquid.
  - This tendency is not consistent with experiments.

**Phase change in the reservoir should be modeled.**

## The one-dimensional model of an LHP was developed.

- Time lag can be reproduced.
  - The change of the position where the condensation starts can be calculated.
  - One-dimensional condensation model was proposed.
- 
- Future works
    - Revising the condensation model
    - Considering the phase change in the reservoir
    - Validation