



Aerothermodynamic Optimization and Design Analysis of a Novel Reusable Launch Vehicle using Numerical Techniques

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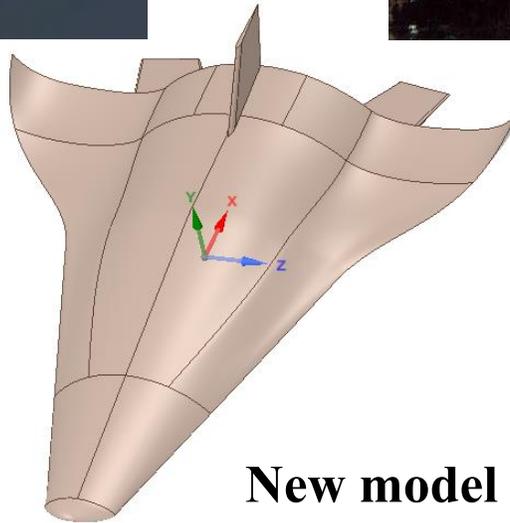
Introduction



HTV



Martin X-33



**New model
RLV**



Literature Review



Title	Author names	Main Focus	Year	Numerical Or Experimental
<p>Aerodynamic and Aeroheating Computations for Wind Tunnel and Flight Conditions XÐ33</p> <p>Aerodynamic and Aeroheating Computations for Wind Tunnel and Flight Conditions</p>	<p>Brian R. Hollis, Richard Thompson, Kelly J. Murphy, Robert J. Nowak, Christopher J. Riley, William A. Wood and Stephen J. Alter</p>	<p>Hypersonic CFD studies validate essential technologies for experimental Single-Stage-to-Orbit craft.</p>	<p>1999</p>	<p>Both.</p>
<p>Aerothermodynamic Optimization of Hypersonic Vehicle TPS Design by a POD/RSM-Based Approach</p>	<p>P.C. Chen¹, D.D. Liu², K.T. Chang³, L. Tang³, X.W. Gao³, Amarshi Bhungalia⁴ Phil Beran⁵, Wei Shyy⁶</p>	<p>This paper describes TPS design using POD/RSM aerodynamic method.</p>	<p>2006</p>	<p>Both</p>
<p>Aerothermal Characterisation of a Typical Re-entry Module in Hypersonic Flow Regime</p>	<p>Devashish Bhalla² , G. Vidya¹ , Manoj T. Nair²</p>	<p>Thermal characteristics of a re-entry module flow field are analyzed.</p>	<p>2021</p>	<p>Both</p>

<p>A study on heat flux predictions for re-entry flight analysis</p>	<p>Raman Balu, A.R.Arnalt Stalin ,Prince Raj L</p>	<p>analysis of heat transfer occurring at hypersonic and hyper velocity flow regimes over re-entry configurations</p>	<p>2012</p>	<p>Numerical</p>
<p>Aerothermal environment definition for a reusable experimental re-entry vehicle wing</p>	<p>Francesco Battista¹, Giuseppe C. Rufolo², Marco Di Clemente³</p>	<p>A simplified methodology is developed to evaluate wing aerothermal environment.</p>	<p>2007</p>	<p>Both but mostly numerical</p>
<p>An aerothermodynamic design optimization framework for hypersonic vehicles</p>	<p>Simone Di Giorgio, Domenico Quagliarella, Giuseppe Pezzella, Sergio Pirozzoli</p>	<p>A highly integrated design environment is developed for aerothermodynamic optimization.</p>	<p>2018</p>	<p>Experimental</p>



Literature Review



Constrained Optimization of Three-Dimensional Hypersonic Vehicle Configurations	Scott G. Sheffer 1 and George S. Dulikravich 2	A constrained shape optimization procedure is presented.	1993	Both
Multidisciplinary optimization of airbreathing hypersonic vehicles	Kevin G. Bowcutt	An MDO design system was developed combining propulsion, aerodynamics, mass properties, and modeling. optimization of a hypersonic cruise missile to maximize overall mission range	2001	Both
Rapid supersonic/hypersonic aerodynamics analysis model for arbitrary geometries	Marcus A. Lobbia	A unique implementation of supersonic/hypersonic analysis techniques is developed for automation.	2016	Experimental



Literature Review



Aeroelastic and Aero thermoelastic Analysis of Hypersonic Vehicles	Jack J. McNamara* and Peretz P. Friedmann	the objective of this paper is to survey the status of research in the area of hypersonic aeroelasticity and aerothermoelasticity.	2006	Numerical
Calculation of Heat Transfer and Drag Coefficients for Aircraft Geometric Models	Victor V. Kuzenov 1, Sergei V. Ryzhkov 1, and Aleksey Yu. Varaksin	An algorithm for heat fluxes and transfer coefficient calculations is developed.	2022	Numerical
Aerodynamic performance analysis of a winged re-entry vehicle from hypersonic down to subsonic speed	Giuseppe Pezzella, Antonio Viviani	phase-A design level of a reusable and unmanned flying laboratory designed to perform a high lift return from low Earth orbit	2016	Both
Design and CFD Analysis on the Reduction of Thermal Effect in Re-entry Vehicle by Using Retractable Aerospike	Konstantin Volkov	The study's goal was to perform a thermos-structural analysis of the TPS of a re-entry module known as the Crew module	2022	Both
AEROHEATING ANALYSIS FOR PLANETARY RE-ENTRY VEHICLES	Alvin Murray	A process for predicting the aero heating and thermal response of blunt re-entry configurations in high-speed flows	2003	Numerical



Literature Review



DRAG REDUCTION FOR HYPERSONIC RE-ENTRY VEHICLES	G. Gopala Krishnan, Akhil and Nagaraja S R	A numerical study on re-entry vehicles with spikes from the point-of view of drag reduction	2017	Numerical
Aerodynamic design exploration for reusable launch vehicle using genetic algorithm with Navier stokes solver	By Tomoaki TATSUKAWA1), Taku NONOMURA2), Akira OYAMA2) and Kozo FUJII2	A genetic algorithm with Navier-Stokes solver is used to analyze aerodynamic characteristics.	2012	Experimental
Hypersonic and High-Temperature Gas Dynamics	JOHN D. ANDERSON JR		2019	

Introduction

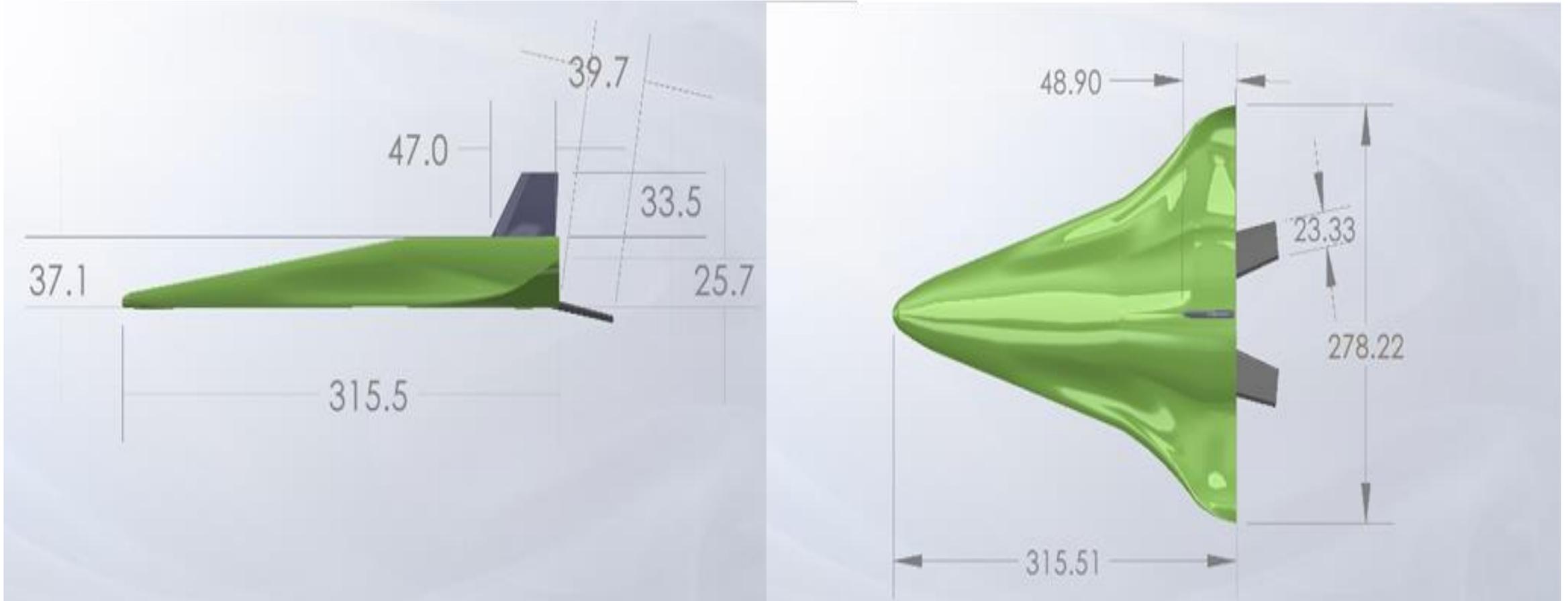
- With the growth of space exploration and commercial travel, the development of efficient and reliable reentry vehicles has become increasingly important to provide improved aerodynamic features, thermal protection, weight reduction, and cost minimization through enhanced blunt-nose designs, resulting in increased payload capacity and extended mission durations.
- The optimization of these designs is particularly vital for reusable spacecraft, as their lifespan and sustainability are extended.
- Numerical analysis, like CFD, accurately simulates real-life flight conditions by solving complex fluid flow, heat transfer, and pressure equations, allowing engineers to predict aerothermal and aerodynamic behaviors with precision, which informs the reliable design and optimization of flight vehicles across various scenarios.
- Therefore, in recent years, numerical studies have become very popular among researchers to experiment and develop more efficient RLV designs.

Design unique RLV
inspired by HTV and
X-33

Conduct numerical
study to predict
accuracy of its
aerothermal
behaviors.

Perform
mathematical
analysis to examine
the aerodynamic
heating

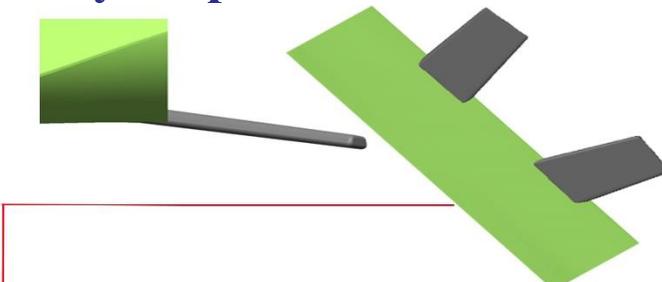
Validating the model
w.r.t the reference
papers.



vertical stabilizer (fin)

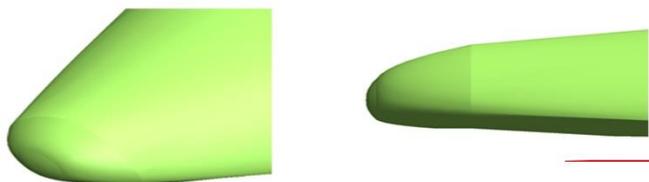
- Provide drag and Yaw controllability at hypersonic speed and also during landing.

Body Flaps



- Provide more aerodynamic trim
- Maintaining Lift/Drag Ratio
- Provide more control (steering, descent, and landing)

Blunt nose



- Reducing heat transfer rates
- Mitigating kinetic heating

Winglet



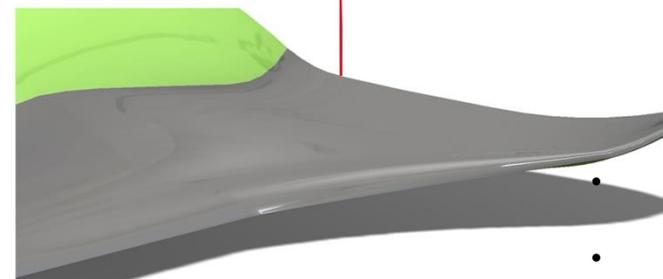
- Separation of Heat and Air Flow
- Provides Controllability with more gliding capability
- Reduces Vortex at the tip

Slender Fuselage



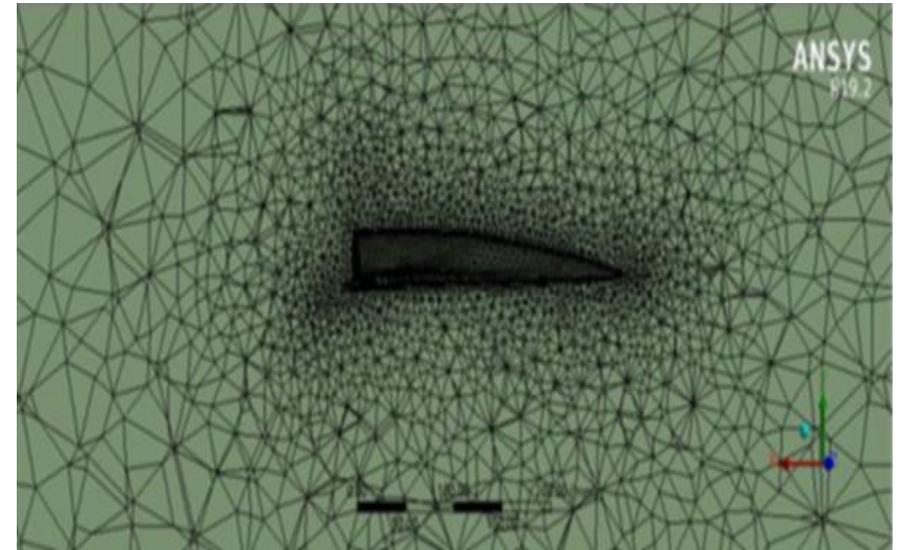
- Provides a more rigid body to accommodate devices and lower heat transfer rate.
- Overall aerodynamic control
- Lower drag, higher lift, and Reduction of weight
- Reduction of fluid density over vehicle surface wall.

High Cambered airfoil



- Provide more lift during landing
- More stability
- Higher lift/Drag ratio reduces speed while re-entering the atmosphere

Names	Description
Grid size	90mm
Face sizing	80 mm
Inflation	first layer
Elements	671492
Nodes	195040
Mesh method	Tetrahedron
Orthogonal quality	0.051
First layer thickness	2.26E-05
Reynold number	7.89E+06
Kinematic viscosity m ⁴ /s	8.012E-04
Y+	1



3D design of RLV

Grid Independence Test

Turbulence Model Validation Check

- Aerodynamic heating analysis calculating Fay-Riddle stagnation point heat transfer coefficient

Names	Description
Solver	Steady-state, density based, energy equation
Air density	Ideal Gas
Air viscosity	Sutherland coefficients three
Turbulence model	K- ω SST
Scheme	AUSMD implicit
Courant	0.35
Convergence criteria	10^{-5}
Iterations	5000

Continuity equation

$$\frac{\partial \rho}{\partial t} + \frac{\partial(\rho u)}{\partial x} + \frac{\partial(\rho v)}{\partial y} + \frac{\partial(\rho w)}{\partial z} = 0 \quad (1)$$

x momentum equation

$$\rho \frac{\partial u}{\partial t} + \rho u \frac{\partial(u)}{\partial x} + \rho v \frac{\partial(u)}{\partial y} + \rho w \frac{\partial(u)}{\partial z} = -\frac{\partial p}{\partial x} \quad (2)$$

y momentum equation

$$\rho \frac{\partial v}{\partial t} + \rho u \frac{\partial(v)}{\partial x} + \rho v \frac{\partial(v)}{\partial y} + \rho w \frac{\partial(v)}{\partial z} = -\frac{\partial p}{\partial y} \quad (3)$$

z momentum equation

$$\rho \frac{\partial w}{\partial t} + \rho u \frac{\partial(w)}{\partial x} + \rho v \frac{\partial(w)}{\partial y} + \rho w \frac{\partial(w)}{\partial z} = -\frac{\partial p}{\partial z} \quad (4)$$

Energy

$$\frac{\partial s}{\partial t} + u \frac{\partial(s)}{\partial x} + v \frac{\partial(s)}{\partial y} + w \frac{\partial(s)}{\partial z} = 0 \quad (5)$$

For a calorically perfect gas can be replaced by the following equation-

$$\frac{\partial}{\partial t} \left(\frac{p}{\rho^\gamma} \right) + u \frac{\partial}{\partial x} \left(\frac{p}{\rho^\gamma} \right) + v \frac{\partial}{\partial y} \left(\frac{p}{\rho^\gamma} \right) + w \frac{\partial}{\partial z} \left(\frac{p}{\rho^\gamma} \right) = 0 \quad (6)$$

$$\rho \left[\frac{\partial V}{\partial t} + (V \cdot \nabla) V \right] = -\nabla P + \nabla \cdot [\lambda(\nabla \cdot V)\bar{I}] + \nabla \cdot [\mu(\nabla V + \nabla V^{tr})] \quad (7)$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho V) = 0 \quad (8)$$

$$\rho C_p \left[\frac{\partial T}{\partial t} + (V \cdot \nabla) T \right] = \nabla \cdot (k \nabla T) + \frac{\partial \rho}{\partial t} + (V \cdot \nabla) P + \Phi \quad (9)$$

$$P = \rho R T \quad (10)$$

$$\Phi = \lambda(\nabla \cdot V)^2 + \frac{\mu}{2} (\nabla V + \nabla V^{tr})^2 \quad (11)$$

$$C_l = \frac{L}{0.5 \rho v^2 S_{ref}} \quad (12)$$

$$C_d = \frac{D}{0.5 \rho v^2 S_{ref}} \quad (13)$$

$$C_m = \frac{M}{0.5 \rho v^2 l_{ref} S_{ref}} \quad (14)$$

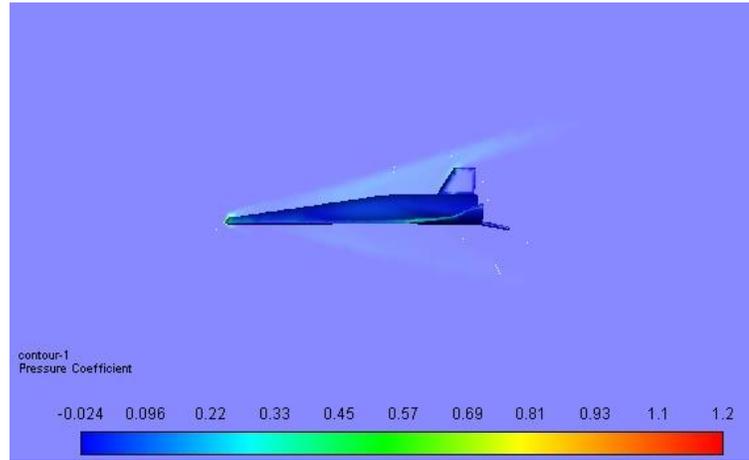
- Calculating the Fay-Riddell equations is essential for analyzing aerodynamic heating at the stagnation point during hypersonic re-entry.
- These equations offer a way to estimate the heat transfer rate at the stagnation point of a reentry vehicle traveling at hypersonic speeds.
- The Fay-Riddell equation is commonly used to validate contemporary computational fluid dynamics (CFD) solutions, serving as a reliable benchmark due to its accuracy in predicting heat flux.
- The modified versions of the equations provided by Fay and Riddell [26] are as follows—

$$h = 0.94K_1(\rho_s\mu_s)^{0.4}(\rho_w\mu_w)^{0.1} \sqrt{\left(\frac{dU}{dx}\right)_{x=0}} \quad (15)$$

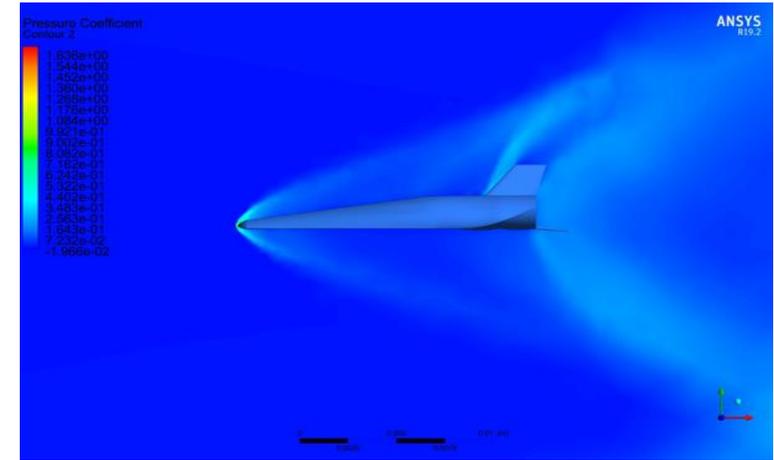
$$\left(\frac{du_e}{dx}\right)_s = \frac{1}{Re_{eff}} \sqrt{\frac{2(p_s - p_\infty)}{\rho_s}}$$

$K_1 = 1$ for the axisymmetric body,
 ρ_s is static density,
 ρ_w is wall density,
 μ_s is the viscosity at the static condition and
 μ_w is the viscosity of the wall.

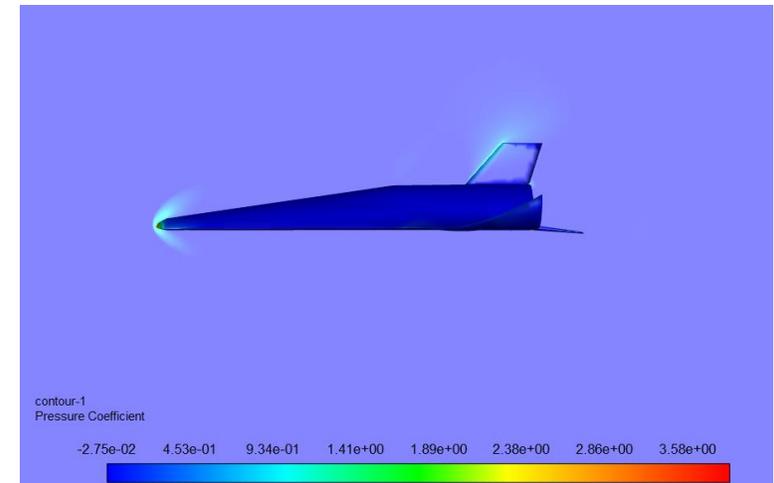
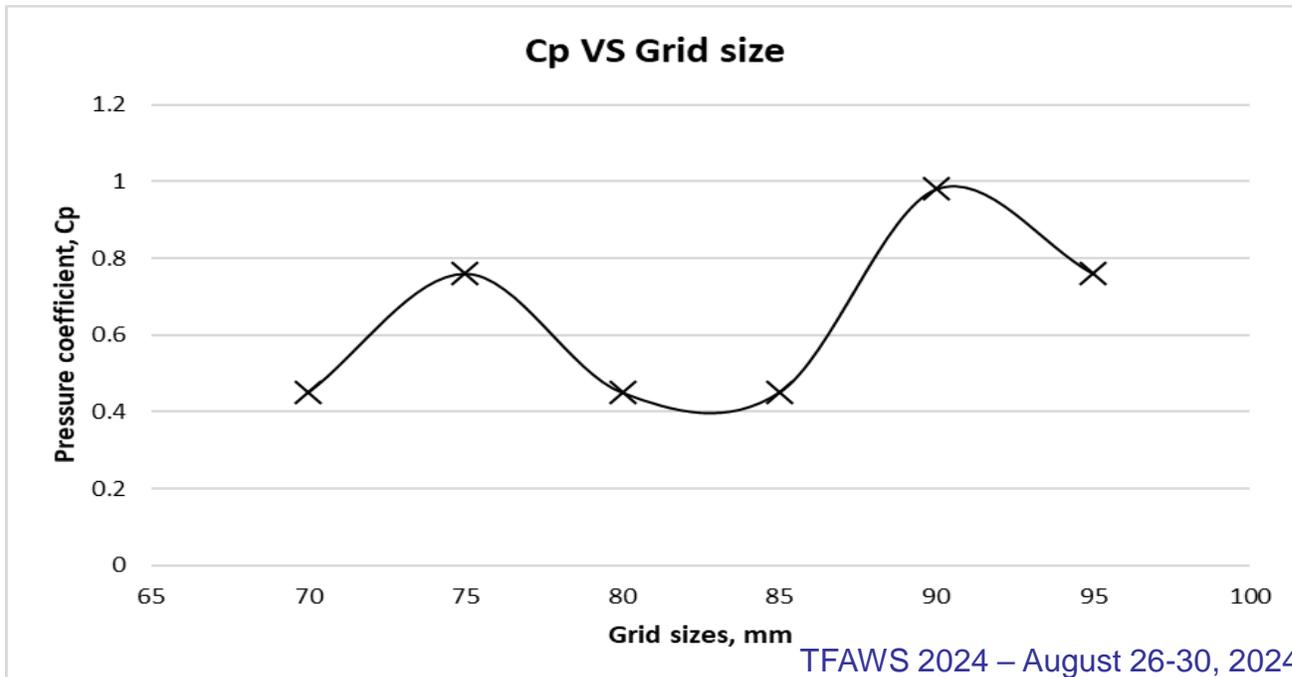
Edge Sizing Element Size	Face Sizing 2 Element Size	Mesh Elements
mm	mm	
65	65	314270
70	70	421512
75	75	314270
75	75	314270
80	80	320738
85	85	421512



(a) Grid Quantity 0.31M

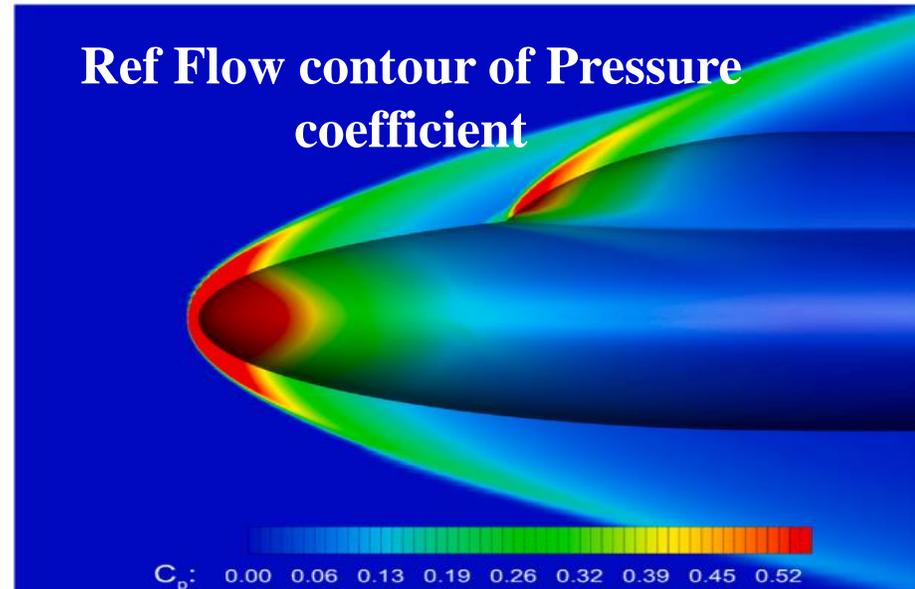
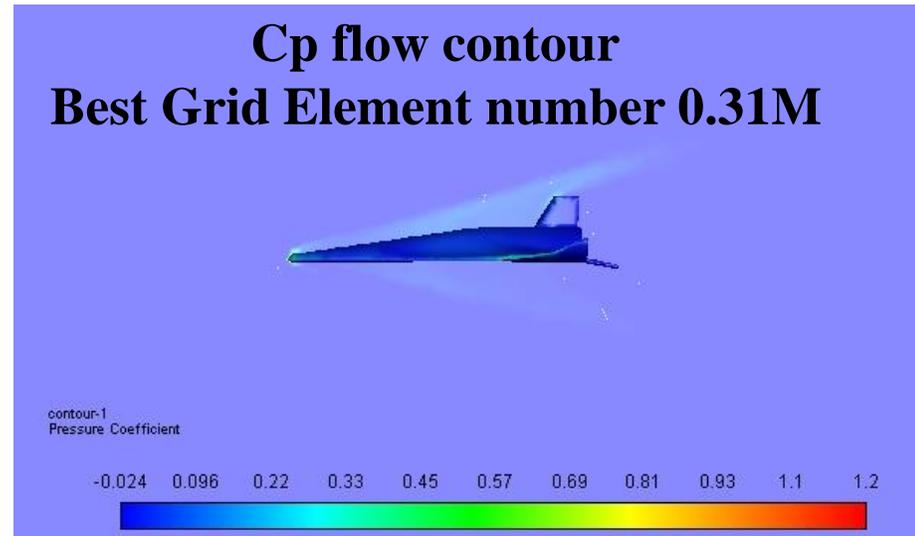


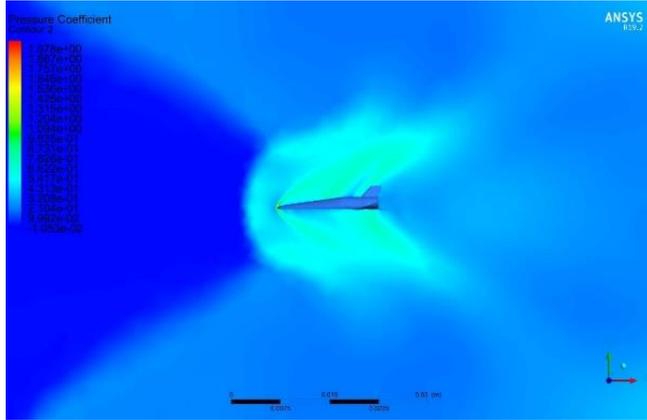
(b) Grid Quantity 0.32M



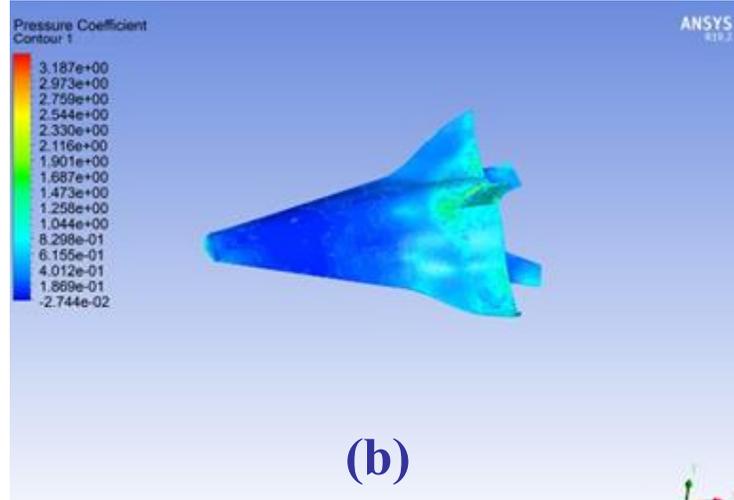
(c) Grid Quantity 0.42M

Obtained data		Ref Data	
Mesh Elements	Cp	Cp	Error%
0.31 M	0.49	0.52	6.122449
0.42 M	0.76	0.52	-31.5789
0.32 M	0.98	0.52	-46.9388

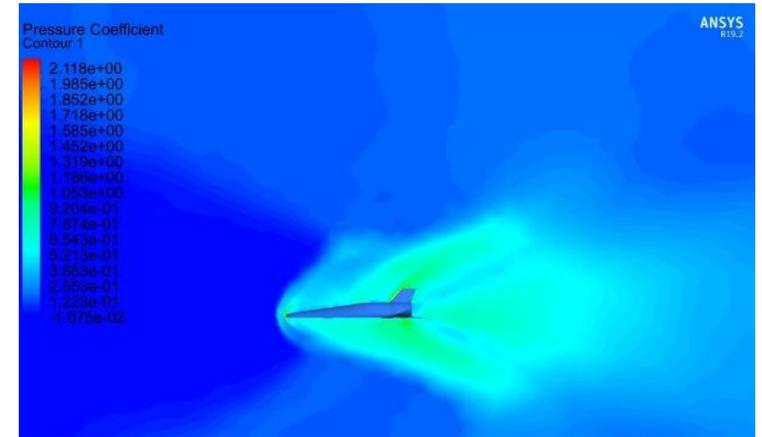




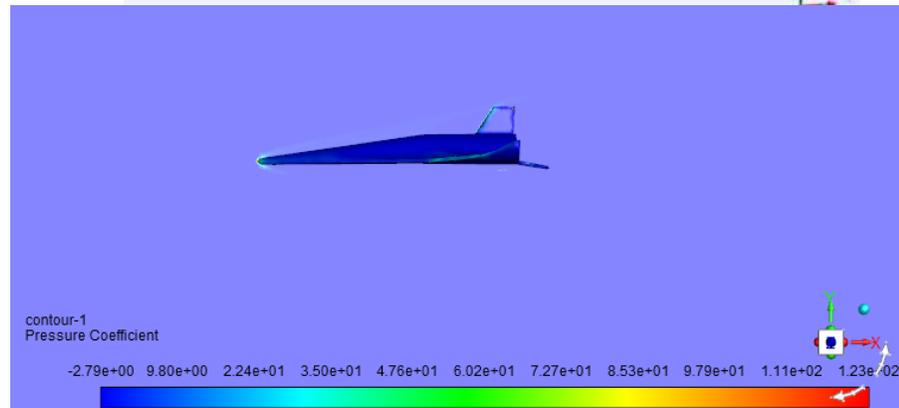
(a)



(b)

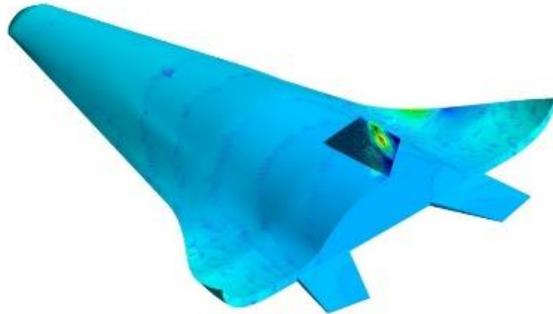
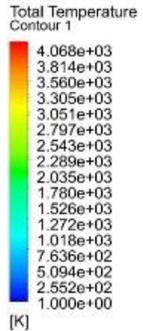


(c)

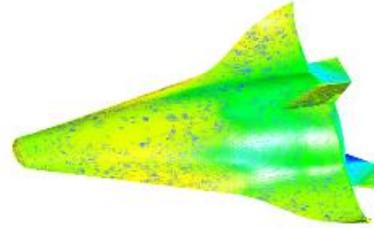
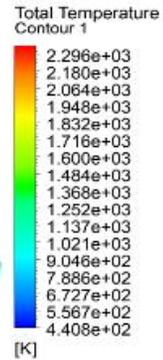
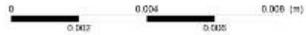


(d)

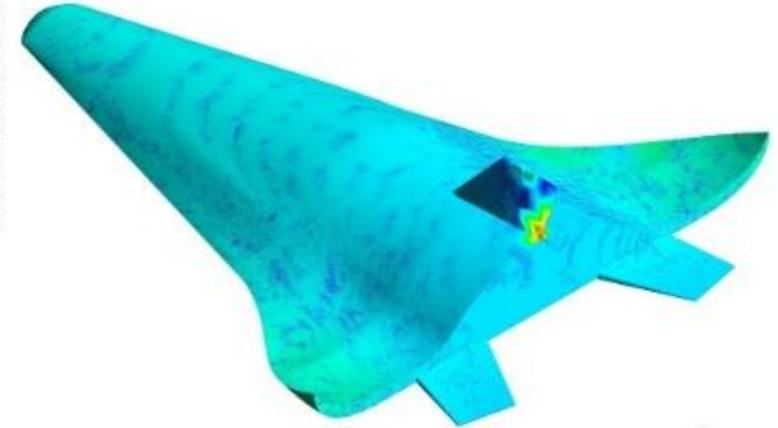
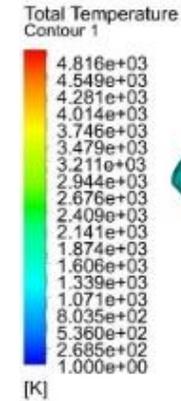
Variation of Pressure Coefficient for Turbulence Models (a) K-w SST, (b) K-e Realizable, (c) K-e Standard, and (d) LES



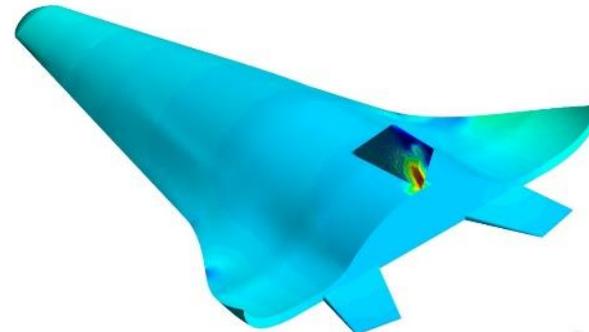
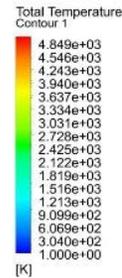
(a)



(b)



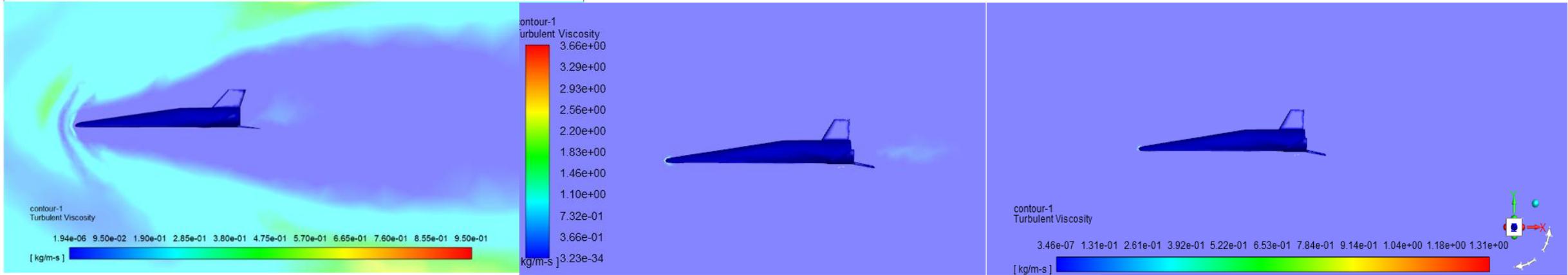
(c)



(d)



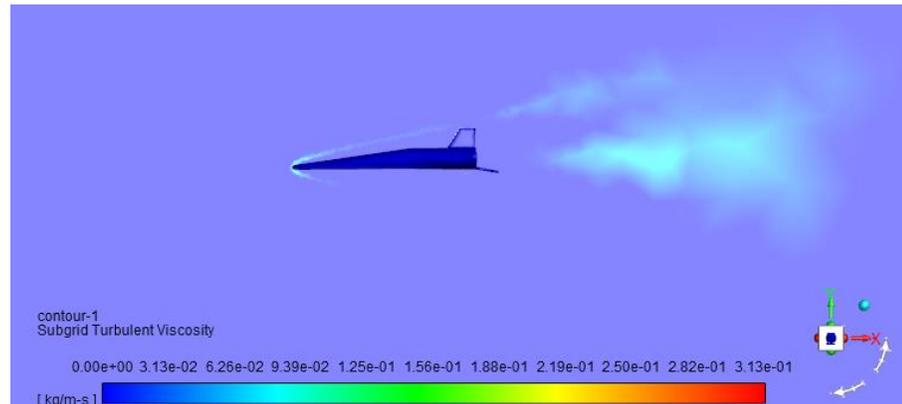
Changes in Total Temperature for Turbulence Models (a) K-w SST, (b) K-e Realizable, (c) K-e Standard, and (d) LES



(a)

(b)

(c)



(d)

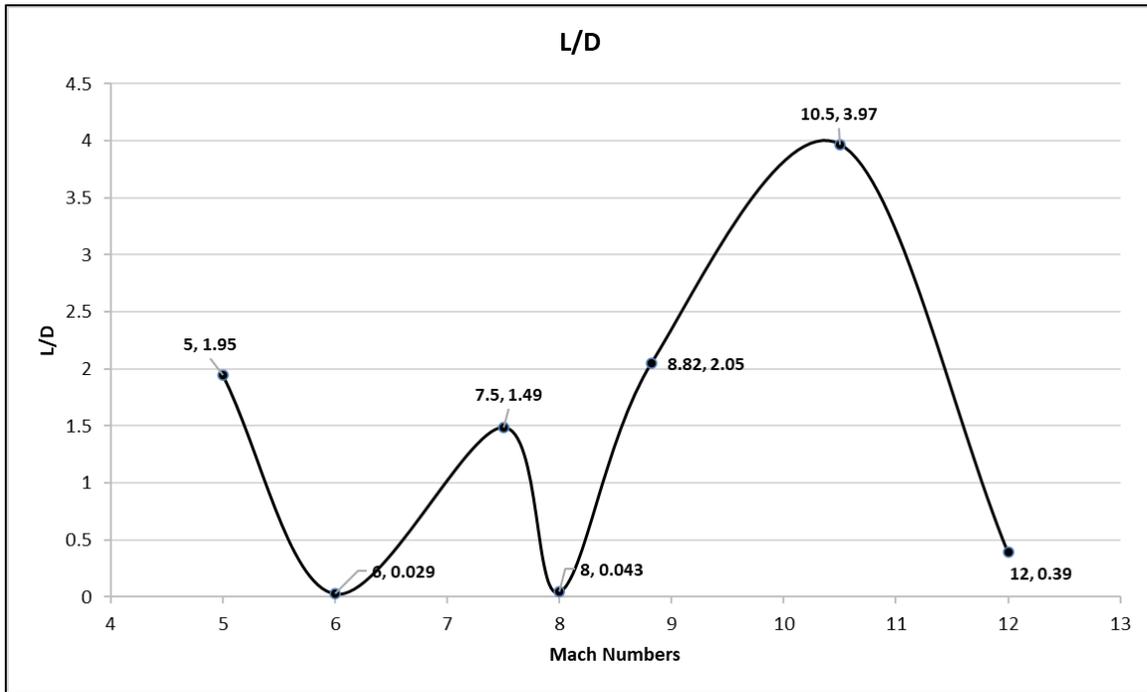
Changes in Turbulence Viscosity for Turbulence Models (a) K-w SST, (b) K-e Realizable, (c) K-e Standard, and (d) LES



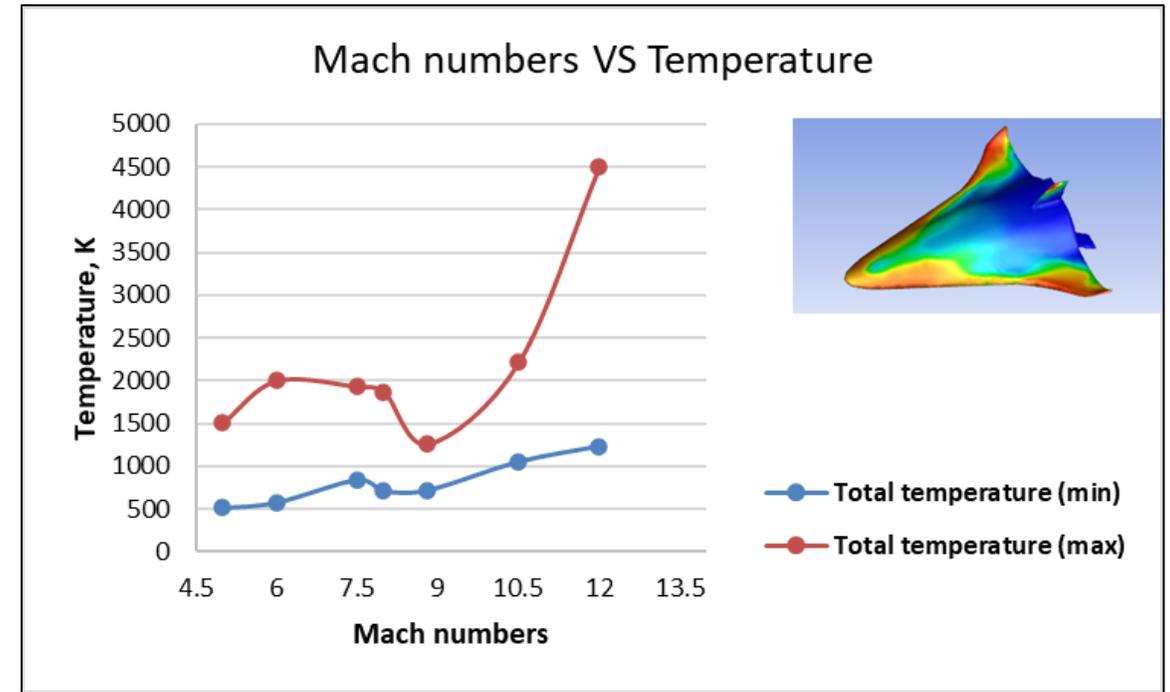
Aerodynamic Heating Analysis for Different Mach Cases



Mach M	Pressure P Pa	Density, kg/m³ ρ_e	Viscosity μ_e	Velocity, m/s V_∞	Temperature, K T_∞
5	1196.22	1.84E-02	1.47E-05	1.70E+03	2.26E+02
6	5529.1	1.23E+00	1.42E-05	2040	216.65
7.5	5529.1	0.0081	1.47E-05	2550	216.65
8	1127.6	0.0081	1.42E-05	2720	252.1
8.82	98635.61	7.07E-04	1.42E-05	2887.3	267
10.5	121000	1.99E-05	1.10E-05	3570	227
12	1.0365	1.99E-05	1.10E-05	4080	180.65



Lift-to-Drag Ration VS Mach numbers

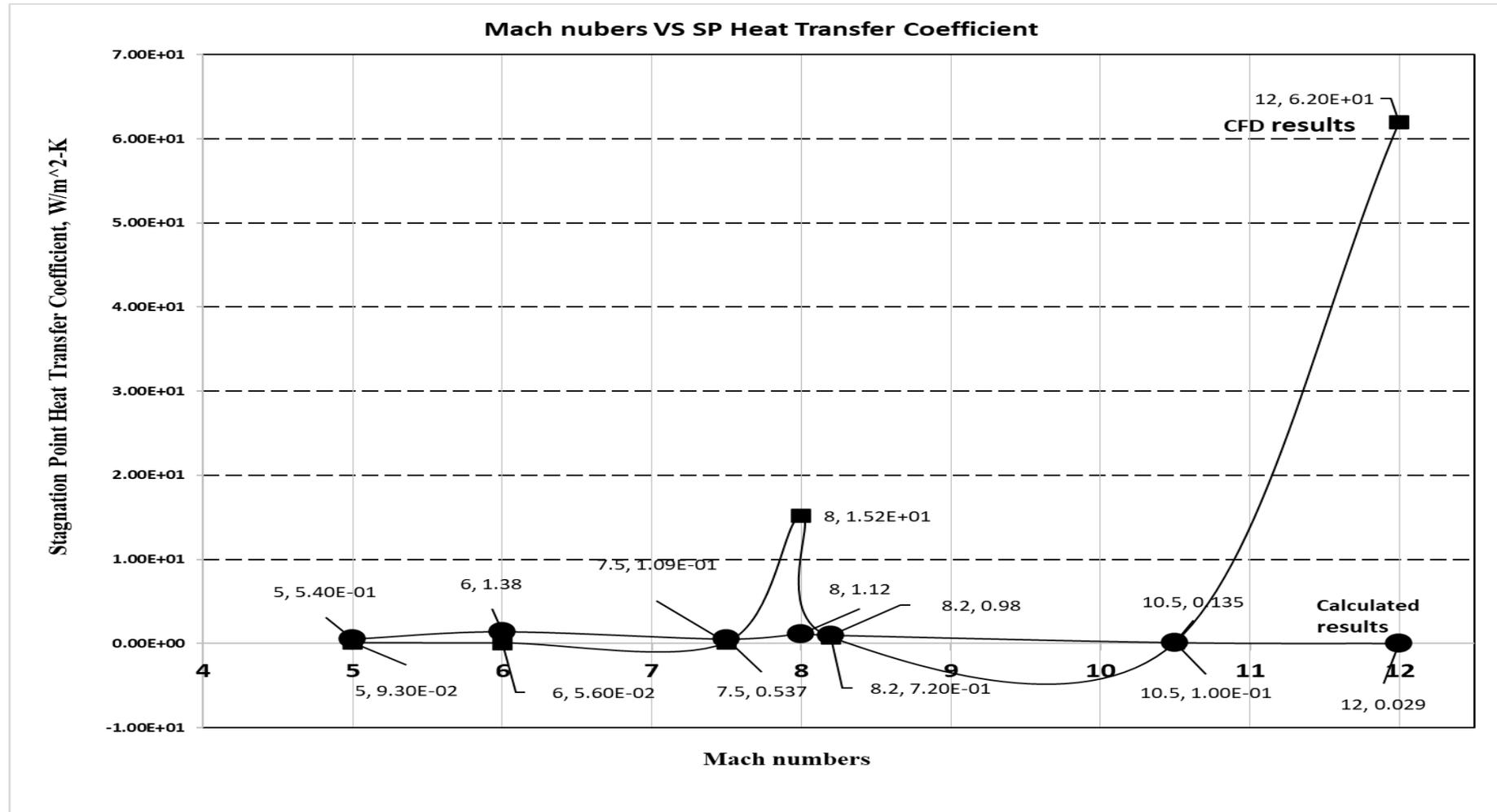


Mach numbers VS Total Temperature at different positions (a) Nose and (b) Body

List of Variables used to calculate stagnation point heat transfer coefficient

Mach	Density ρ_e	Density (wall) ρ_w	Viscosity μ_e	Viscosity wall μ_w	Velocity, m/s V_∞	Enthalpy $h_{e,s}$	R-eff (ref nose radius, m)	Temperature T_∞	Velocity gradient DV/Dx	SP Heat Transfer Coefficient
5	1.84E-02	2719(default)	1.47E-05	1.78E-05	1.70E+03	1.82E+06	2.70E-03	2.26E+02	1.34E+05	0.54
6	1.23E+00	2719(default)	1.42E-05	1.78e-05(default)	2040	1822323	0.0027	216.65	3.13E+04	1.38
7.5	0.0081	2719(default)	1.47E-05	1.78e-05(default)	2550	1822323	0.0027	216.65	2.56E+05	0.537
8	0.0081	2719(default)	1.42E-05	1.78e-05(default)	2720	1822323	0.0027	252.1	1.15E+06	1.12
8.82	7.07E-04	2719(default)	1.42E-05	1.78e-05(default)	2887.3	1822323	0.0027	267	6.13E+06	0.98
10.5	1.99E-05	2719(default)	1.10E-05	1.78e-05(default)	3570	1822323	0.0027	227	2.50E+06	0.135
12	1.99E-05	2719(default)	1.10E-05	1.78e-05(default)	4080	1822323	0.0027	180.65	118944.7	0.029

Comparison between obtained stagnation point heat transfer from CFD and Calculated Stagnation point heat transfer coefficient at different Mach cases



Conclusion

The blunt nose effectively reduced peak temperatures by generating a detached shock wave and turbulent wake, leading to lower heat transfer intensity.

The K- ω SST turbulence model, used with an optimal grid size of 0.31 million elements, provided the most accurate predictions for both aerodynamic behaviours and thermal management

At Mach 10.5, the model achieved higher lift-to-drag ratios, enhancing altitude sustenance and reducing thermal stress on the Thermal Protection System (TPS)

The model demonstrated better thermal management with reduced heat transfer coefficients and peak temperatures compared to traditional designs.

The overall design improvements validated the model's superior performance in high-speed flight conditions, showcasing its effectiveness in both aerodynamic and thermal evaluations.



Acknowledgement

I wish to extend my heartfelt thanks to my supervisor, Prof. Srinivas G., Associate Professor, for the opportunity to work on this outstanding project. His invaluable guidance, patience, encouragement, enthusiasm, and extensive knowledge were instrumental in successfully completing my research. This project has significantly enhanced both my research and technical skills. Additionally, I am deeply grateful to my parents and loved ones for their unwavering love, prayers, and constant support, which have motivated me to achieve my goals.



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Any Questions?



Thank You